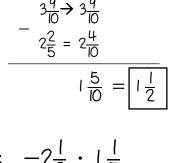
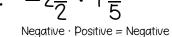
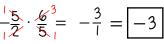
<u>Rational</u>	Number: a number that is the quotient of two int	egers	
<u>Operatic</u>	ons with Rational Numbers		
l. 2. 3.	ng/Subtracting Rational Numbers: Use integer rules to determine whether to add or subtract Find a common denominator. Add or subtract numerators and keep denominator the same. Simplify if necessary. Use integer rules to determine the sign of the		$-2\frac{2}{5} + 3\frac{9}{10}$ $ative + Positive \rightarrow Subtempositive + Subtempositive + 2000 \text{Subtempositive} + 20000 \text{Subtempositive} + 2000 \text{Subtempositive} + 2000 Subtempos$
• <u>Mult</u> I. 2. 3. 4. 5.	answer. <u>iplying Rational Numbers</u> : Convert mixed numbers to improper fractions. Cross-simplify, if possible. Multiply numerators and multiply denominators. Simplify if necessary Use integer rules to determine the sign of the answer	ex:	$-2\frac{1}{2} \cdot 1\frac{1}{5}$ Negative · Positive = $-\frac{15}{2} \cdot \frac{6}{5} = -\frac{3}{7}$
• <u>Divic</u> 1. 2.	ling Rational Numbers: Convert mixed numbers to improper fractions. Flip second fraction to its reciprocal and change division sign to multiplication	ex:	$-4\frac{1}{4} \div (-1)$ Negative ÷ Negative ÷ $-\frac{17}{4} \div (-\frac{4}{1})$

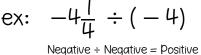
3. Multiply the fractions (as above)











$\rightarrow -\frac{17}{4} \cdot \left(-\frac{1}{4}\right) = \frac{17}{16} = \boxed{1\frac{1}{16}}$

Square Roots

Perfect Square: a number that is the product of a rational number multiplied by itself

ex:

Finding the square root of a number is the opposite of squaring a number. Find the number that you can multiply by itself to equal the given number.

ex: Find the square root Find the square root of the numerator & denominator: $q = 3^2$, so $\sqrt{q} = 3$ $64 = 8^2$, so $\sqrt{64} = 8$ 3 = 8

Determine whether the number is rational or irrational.

183	2. √5	3. π	4. <u>7</u> <u>3</u>

Evaluate each numerical expression.

$5\frac{4}{5} + \left(-\frac{3}{10}\right)$	6. $2\frac{3}{4} - 5\frac{1}{2}$	7. $-\frac{11}{15} \cdot \left(-\frac{10}{33}\right)$	8. $\frac{6}{7} \div (-4)$
$q. \ 6\frac{2}{3} + \left(-q\frac{2}{q}\right)$	$104\frac{1}{5} \div \left(-2\frac{1}{7}\right)$	11. $8\frac{2}{3} \cdot \left(-1\frac{2}{13}\right)$	12. $-3\frac{7}{12} - 5\frac{1}{8}$

Find each square root.

13. √25	14. –√144	15. √225	I6. −√ 36
I7. √I2I	I8. √ IOO	$19. \sqrt{\frac{1}{4}}$	$20\sqrt{\frac{49}{81}}$
		$\sqrt{4}$	$-\sqrt{81}$

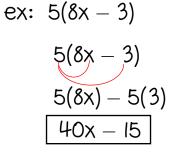
Evaluating Algebraic Expressions

- I. Substitute the given values for the variables in the expression
- 2. Evaluate the expression using the order of operations
 - · Parentheses/Brackets (inside to outside)
 - Exponents
 - Multiplication/Division (left to right)
 - Addition/Subtraction (left to right)

ex: evaluate $9x^2 - 4(y + 3z)$ for x = -3, y = 2, z = 5 $9(-3)^2 - 4(2 + 3 \cdot 5)$ $9(-3)^2 - 4(2 + 15)$ $9(-3)^2 - 4 \cdot 17$ $9 \cdot 9 - 4 \cdot 17$ $81 - 4 \cdot 17$ 81 - 68 = 13

The Distributive Property

- 1. Multiply the number outside the parentheses by each term in the parentheses.
- 2. Keep the addition/subtraction sign between each term.



Simplifying Algebraic Expressions

- 1. Clear any parentheses using the Distributive Property
- 2. Add or subtract like terms (use the sign in front of each term to determine whether to add or subtract)
- ex: 2(3x 4) 12x + 9 2(3x - 4) - 12x + 9 6x - 8 - 12x + 9-6x + 1

Evaluate each expression for a = 9, b = -3, c = -2, d = 7. Show your work.

21. a – cd	22. 2b ³ + c ²	23. $\frac{a+d-c}{b}$	24. (a – b)² + d(a + c)
25. 4c - (b - a)	26. <mark>a</mark> - 5a	27. 2bc + d(12 – 5)	28. b + 0.5[8 – (2c + a)]

Simplify each expression using the Distributive Property.

29. 5(2g - 8)	30. 7(y + 3)	313(4w – 3)	32. (6r + 3)2

Simplify each expression, showing all work.

33. 8(x + l) - l2x	34. 6w - 7 + 12w - 3z	35. 9n - 8 + 3(2n - 11)	36. 3(7x + 4y) - 2(2x + y)
37. (15 + 8d)(-5) - 24d + d	38. 9(b−1)−c+3b+c	39. 20f - 4(5f + 4) + 16	40. 8(h - 4) - h - (h + 7)

Solving One-Step Equations

- 1. Cancel out the number on the same side of the equal sign as the variable using inverse operations (addition/subtraction; multiplication/division)
- 2. Be sure to do the same thing to both sides of the equation!

Solving Two-Step Equations

- 1. Undo operations one at a time with inverse operations, using the order of operations in reverse (i.e. undo addition/subtraction before multiplication/division)
- 2. Be sure to always do the same thing to both sides of the equation!

ex:
$$-18 = 6j$$

 $-18 = 6j$
 6
 $-3 = j$ $j = -3$

ex: $\frac{a}{7} - 12 = -9$ $\frac{a}{7} - 12 = -9$ + 12 + 12 $7 \times \frac{a}{7} = 3 \times 7$ a = 21

Solving Multi-Step Equations

- 1. Clear any parentheses using the Distributive Property
- 2. Combine like terms on each side of the equal sign
- Get the variable terms on the same side of the equation by adding/subtracting a variable term to/from both sides of the equation to cancel it out on one side
- 4. The equation is now a two-step equation, so finish solving it as described above

ex: 5(2x - 1) = 3x + 4x - 1 10x - 5 = 3x + 4x - 1 10x - 5 = 7x - 1 -7x - 7x 3x - 5 = -1 +5 + 5 3x = 4 $3x = \frac{4}{3}$ $x = \frac{4}{3}$

Solve each equation, showing all work.

		· · · · · · · · · · · · · · · · · · ·	
41. $f - 64 = -23$	42. $-7 = 2d$	43. $\frac{b}{-12} = -6$	44. $13 = m + 21$
		$\frac{1}{-12} = -6$	
	-		
45. $5x - 3 = -28$	46. $\frac{\omega + 8}{-3} = -9$	47. $-8 + \frac{h}{4} = 13$	48. 22 = 6y + 7
	-3 4	$-0 + \overline{4} = 15$	_
49. $8x - 4 = 3x + 1$	50. $-2(5d - 8) = 20$	51. 7r + 21 = 49r	52. $-9g - 3 = -3(3g + 2)$
53. $5(3x - 2) = 5(4x + 1)$	54. $3d - 4 + d = 8d - (-12)$	55. $f - 6 = -2f + 3(f - 2)$	56. $-2(y - 1) = 4y - (y + 2)$

Key Words for Operations:

Addition	Subtraction
 Sum More than Increased by Plus 	DifferenceLess thanDecreased byMinus
Multiplication	Division
 Product Times Multiplied By Twice/Doubled (x2) 	 Quotient Divided By Half (÷2)

Writing Equations:

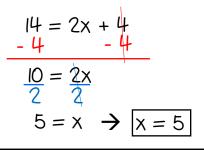
- Translate the equation using key words for operations.
- "Is" translates to =.

ex: Translate to an algebraic expression:

b multiplied by the sum of a and c

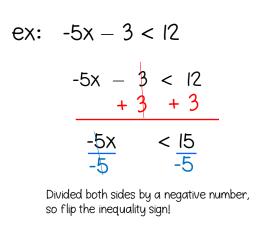
ex: Translate to an equation $\ensuremath{\mathcal{E}}$ then solve:

14 is 4 more than the product of x and 2.

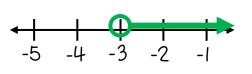


Solving & Graphing Inequalities

- I. Solve the inequality as if it is an equation.
- 2. If you multiply or divide both sides of the inequality by a negative number, flip the inequality sign to the opposite sign.
- 3. Write your answer with the variable to the left of the inequality sign.
- 4. Graph the solution on a number line.
 - Make an open circle on the number if the number is not included in the solution (< or >)
 - Make a closed circle if the number is included (≤ or ≥)
 - Shade to the left for less than (< or ≤)
 - Shade to the right for greater than (> or \geq).







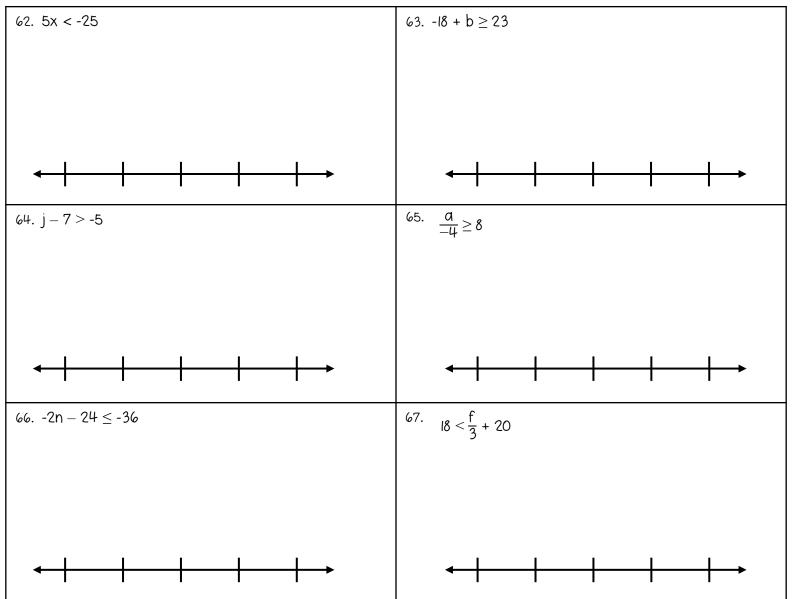
Translate each verbal phrase into an algebraic expression.

57. the difference of w and z	58. g more than the quotient of b and f	59. the product of v and n increased by p cubed

Translate each sentence into an algebraic equation. Then solve the equation.

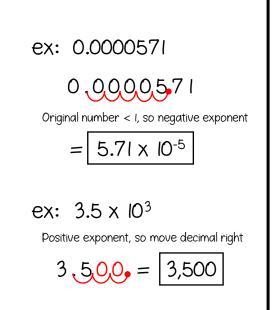
60. Nine is six less negative two.	than the quotient of x and	61.	The sum of y and seven is twice the difference of y and twelve.

Solve each inequality. Then graph your solution on the number line.



<u>Standard Form to Scientific Notation</u>: move the decimal after the first non-zero digit and eliminate any trailing zeros. Multiply by 10 to the power equal to the number of places you moved the decimal point. If the original number was greater than 1, the exponent is positive. If the number was less than 1, the exponent is negative.

<u>Scientific Notation to Standard Form</u>: move the decimal point the number of places indicated by the exponent. If the exponent is positive, move the decimal right. If negative, move left.



Negative Exponents & Simplifying Monomials

<u>Zero Exponent</u>: Any number raised to the zero $ex: y^0 = 1$ power equals 1

<u>Negative Exponent</u>: Move the base to the opposite side of the fraction line and make the exponent positive

Monomial x Monomial: Multiply the coefficients and add the exponents of like bases

<u>Monomial</u> ÷ <u>Monomial</u>: Divide the coefficients and subtract the exponents of like bases

<u>Power of a Monomial</u>: Raise each base (including the coefficient) to that power. If a base already has an exponent, multiply the two exponents

<u>Power of a Quotient</u>: Raise each base (including the coefficient) to that power. If a base already has an exponent, multiply the two exponents

ex:
$$x^{-4} = \frac{1}{x^{4}}$$

ex:
$$(4x^3)(2x^5) = \delta x^8$$

ex:
$$\frac{a}{a^6} = a^{-5} = \frac{1}{a^5}$$

ex:
$$(-2fg^5)^3 = -8f^3g^{15}$$

$$\operatorname{ex:} \left(\frac{5d^3}{c}\right)^2 = \frac{25d^6}{c^2}$$

Convert each number to Scientific Notation.

68. 67,000,000,000	69. 0.0009213	70. 0.0000000004	71. 3,201,000,000,000,000

Convert each number to Standard Form.

72. 5.92 x 10 ⁻⁵	73. I.I x 10 ⁷	74. 6.733 x Ю⁻ ⁸	75. 3.27 x 10 ²

Simplify each expression. Write your answers using only positive exponents.

76. ω ^{.q}	77. <u>m⁵</u> m ²	78. f ⁵ · f ³	^{79.} $\left(\frac{h^2}{g}\right)^3$
δ0. (α ⁵) ²	81. <u> </u> b ⁻³	82. z ⁰	83. 4r ⁶ · 3r · 2r ²
^{84.} $\frac{qp^{-2}}{3q^{-3}}$	^{85.} <u>8d³</u> 2cd ⁻²	86. (g ⁴ h) ² · (2g ³ h ⁻¹) ²	87. (6a) ⁰
88. (-3n²k ⁴)²	^{89.} $\left(\frac{\omega^5 x^{-2} y}{\omega^2 x y^4}\right)^3$	90. <u>6 · 107</u> 2 · 103	91. (1.5 · 10 ⁻⁶) · (4 · 10 ⁹)

Finding the Slope Given Two Points: Use the coordinates from the points in the slope formula:

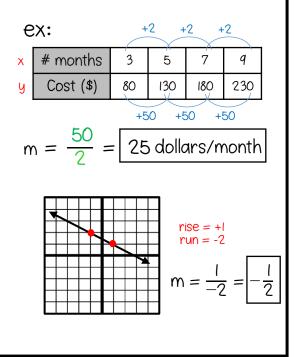
Slope (m) =
$$\frac{y_2 - y_1}{x_2 - x_1}$$

Finding the Rate of Change From a Table: Determine the amount the dependent variable (y) is changing and the amount the independent variable (x) is changing.

Rate of Change = $\frac{\text{change in y}}{\text{change in x}}$

<u>Finding the Slope From a Graph</u>: Choose 2 points on the graph. Find the vertical change (rise) and horizontal change (run) between the 2 points and write it as a fraction $\frac{rise}{run}$. (Up is positive, down is negative, right is positive, and left is negative).

ex: (4, -2), (-3, 8) $m = \frac{8 - (-2)}{-3 - 4} = \frac{10}{-7} = -\frac{10}{7}$



Graphing Linear Equations

Slope-Intercept Form: y = mx + bslope y-intercept

How To Graph:

- I. Make a point on the y-axis at the y-intercept.
- 2. Use the slope to determine where to make the next point. The numerator tells you the rise (how far up/down) and the denominator tells you the run (how far right/left) to make the next point.
- 3. Repeat to make more points and then connect the points with a line.

ex: y = 2x - 4y-intercept: -4 slope: $2 = \frac{2}{1}$ run

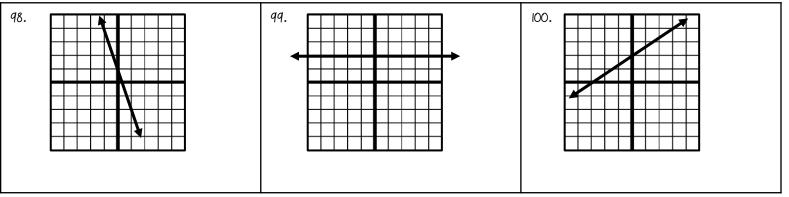
Find the slope of the line that passes through the points. Show your work.

92. (-5, 3), (2, 1)	93. (8, 4), (11, 6)	94. (9, 3), (9, -1)	95. (-4, -2), (-6, 4)			

Find the rate of change. Show your work.

96.	Number of Hours	3	6	9	12		97.	Number of Weeks	I	3	5	7]
	Distance (in miles)	135	270	405	540			Pounds	173	169	165	161	
						-							-

Find the slope of the line.



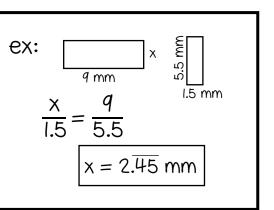
Graph the line.

101. $y = -x - 3$	102. $y = \frac{1}{3}x + 2$	103. $y = -3x - 1$
104. $y = -\frac{3}{2}x - 2$	105. $y = 2x + 1$	106. $y = \frac{1}{4}x$

- I. Set the two cross-products equal to each other
- 2. Solve the equation for the variable

Similar Figures

- 1. To find a missing side length, set up a proportion, matching up corresponding sides.
- 2. Solve the proportion using the steps above.

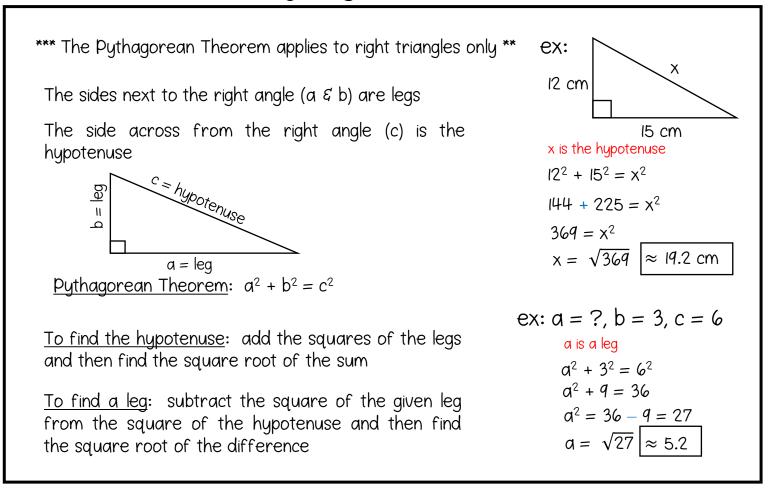


ex: $\frac{m}{4} = \frac{3}{5}$

5m = 12

m = 2.4

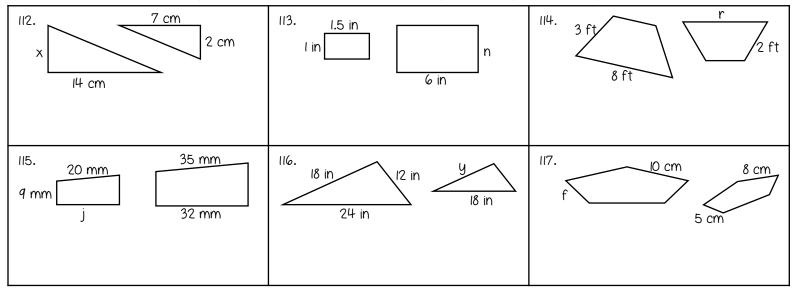
The Pythagorean Theorem



Solve each proportion, showing all work.

$\frac{107.}{7} = \frac{4}{m}$	$\frac{108}{5} = \frac{k}{3}$	$\frac{109}{7} = \frac{8}{2}$	$\frac{10}{n} = \frac{4}{36}$	$\frac{111}{21} = \frac{3}{c}$

Assume each pair of figures is similar. Find the missing side length, showing all work.



Find the missing side length in each right triangle to the nearest tenth. Show your work!

118 a = 6, b = 8, c = ?	119. a=?, b=9cm, c = 13cm	120. a = 7, b = ?, c = 14
1/21. 3 5 X	122. x 10 mm 10 mm	7 in 5 in x

124. A 20-foot ladder is leaning against a wall. The base of the ladder is 5 feet from the wall. How high up the wall does the ladder reach?

Determine whether or not you can form a right triangle from the given side lengths. Explain.

125.	18,	22,	26
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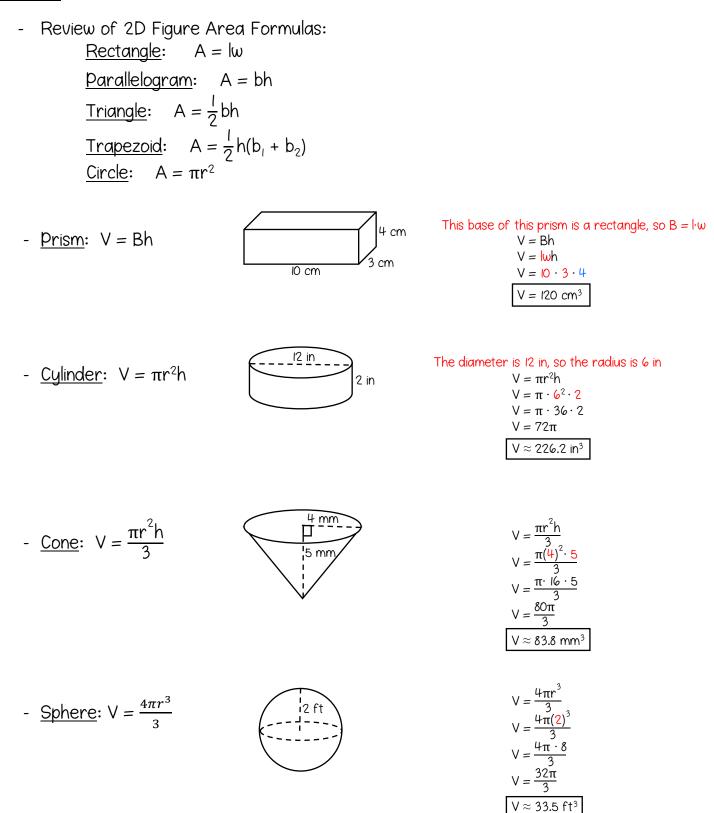
Volume

Volume: the space inside a 3D figure (measured in cubic units)

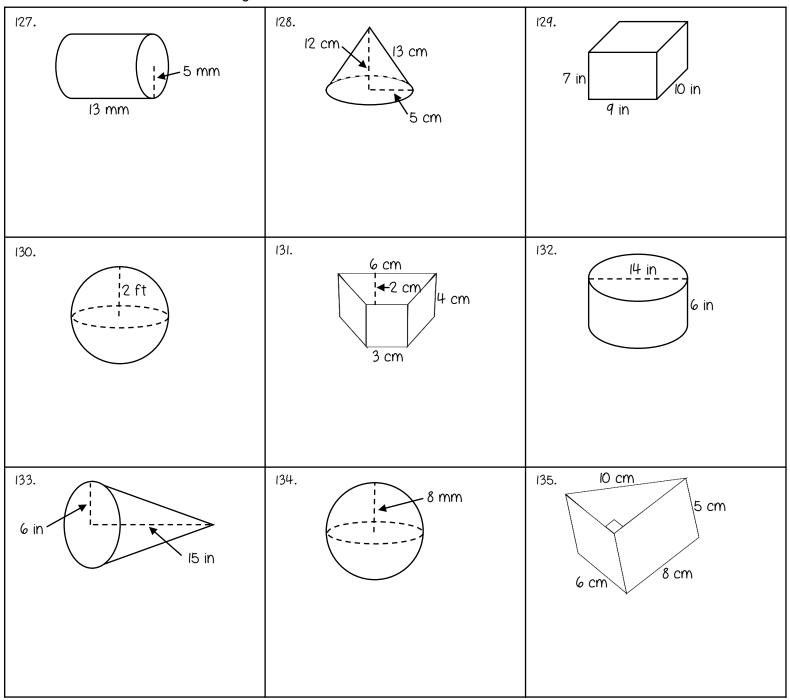
Abbreviations:

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A = area, I = length, w= width, b = base, h = height, r = radius, V = volume, B = area of base
```

Formulas:



Find the volume. If necessary, round to the nearest tenth.



Solve each word problem. Round to the nearest tenth, if necessary.

 136. A cylindrical cup is filled half-way with water. The cup has a diameter of 7 cm and a height of 15 cm. How many mL of water are in the cup? (1 mL = 1 cm³) 	137. A ball with a diameter of 7 cm is placed in a cube- shaped box with 8 cm sides. How much empty space is left in the box?
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